

# AC-DC Bidirectional Single-Phase Step-Down Converter with High Power Factor

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**Abstract** – This paper presents a converter that allows the operation as rectifier or inverter, with high power factor, which the voltage output can be lower, equal or greater than the peak of the input voltage, besides that working with only a cell of conventional switching. The operation stages, equations, control strategy and design of the converter are presented. Finally, simulation results are shown for operation as rectifier and inverter.

## I. INTRODUCTION

Most of the single-stage topologies that allow operating as rectifier have an input AC voltage lower than the output DC voltage. Then, to obtain lower output voltage it is necessary to add another stage as a buck converter, to achieve the voltage magnitude required. Besides, they used at least two switching cells adding losses and diminishing the efficiency of the topology. Among the topologies used at the moment, only one allows the operation with greater or lower voltage in the output converter. This converter was proposed by Cáceres and Barbi [1],[2]. It consists of two individual step-up converters as shown in Fig. 1. In the step-up inverter the load connected in differential mode can theoretically, obtain the output voltage with any value and shape. Besides, respected the condition that individually  $V_{c1}$  and  $V_{c2}$  are greater than  $V_{dc}$ , a degree of freedom exists in the selection of these voltages, where only the difference between them interests to the load.

This way, a sinusoidal output voltage can be obtained with a capacitor with fixed voltage and imposing one sinusoidal variation in the other capacitor, or using two sinusoidal references with a phase-shift of  $180^\circ$  between them, as shown in Fig. 2. Each converter produces a sinusoidal output voltage single-pole with a continuous component, as shows in Fig. 2, with waveforms of  $V_{c1}$  and  $V_{c2}$ . The load is

connected in differential mode between the converters, annulling the continuous components.

The modulation in each converter is  $180^\circ$  degrees phase-shift in relation to the other, it maximizes the excursion of voltage through the load. However, the difference of phase between the two converters can have any value. This is presented as an alternative for the control output voltage of ( $V_{c1}-V_{c2}$ ).

The generation of the bipolar output voltage is obtained by a push-pull arrangement, forcing the converter to operate as source and the another one as load, being bidirectional in current.

Colling and Barbi [4] propose the circuit operating as rectifier. Operating as rectifier it is necessary to invert its

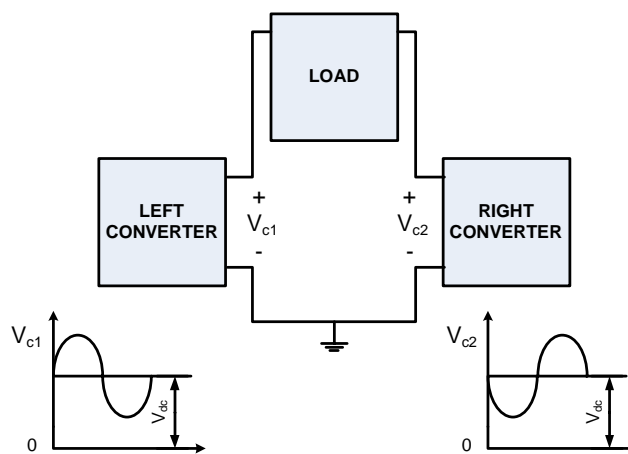


Fig. 2. Basic configuration to get inversion AC-DC [3].

power flow and to establish some control on the absorbed current of AC source. Therefore, an inductor in series with the AC source is included, as shown in Fig. 3. Due to that reversibility of power flow, the elements (inductive and source) are not identified as input or output any more, but as AC-side or DC-side.

This paper proposes a variation of the circuit proposed by Colling and Barbi [4] simplifying the topology presented in Fig. 3.

This simplification consists of substituting the converter of the right side for a capacitor, such modification requires to increase the value of the capacitor, therefore it is able to maintain a higher DC voltage to  $V_{dc}$ . With this, it is possible to diminish the quantity of semiconductors and magnetic elements without modifying the operation of the converter.

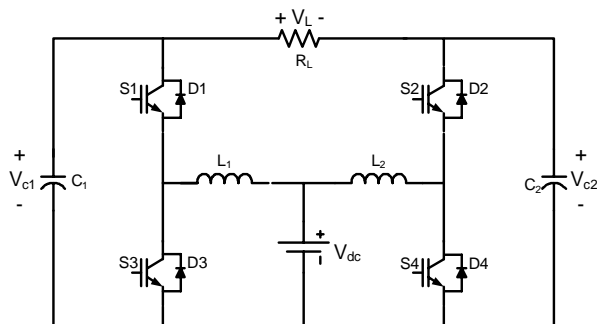


Fig. 1. Basic diagram of the inverter proposed by Cáceres and Barbi [1].

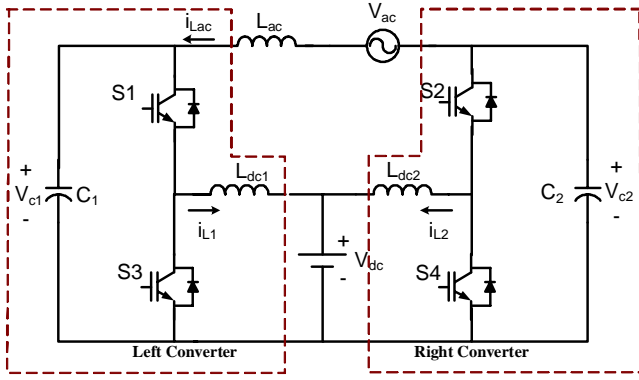


Fig. 3. Rectifier diagram proposed by Colling and Barbi.

## II. TOPOLOGY PROPOSAL

The original topology operating as rectifier is shown in Fig. 3. The function of the converter of the right side consists of keeping a sinusoidal voltage with a DC level, in the capacitor  $C_2$ , greater than  $V_{dc}$ . The voltage in the capacitor  $C_1$ , which it must be complementary to  $V_{c2}$  (Fig. 2), is controlled for the left converter. This also adjusts the value of the current  $i_{Lac}$  to obtain the power factor correction.

The idea of the proposal consists of substituting the right side converter for a capacitor and to control its voltage to follow a DC value. This value must be greater than the output voltage  $V_{dc}$ . Therefore, the function of the left side converter will be to keep a sinusoidal voltage in the  $C_1$  capacitor with one average component, equal to  $V_{c2}$ . The simplified and redesigned circuit is shown in Fig. 4.

This way, in the  $C_1$  capacitor the magnitude of its voltage will be of  $V_{ac} + V_{c2}$ . Therefore, the structure operating as rectifier is similar to a step-down converter, with filter in an input, the difference is that their input voltages have a component alternated above a DC voltage level.

### A. Considerations for the operation of the circuit

The circuit is considered as a step-up inverter voltage. For the  $C_2$  capacitor, its voltage must be (1).

$$v_{c2}^*(t) = V_{c2dc}^* \quad (1)$$

The total sinusoidal excursion will be applied to the  $C_1$

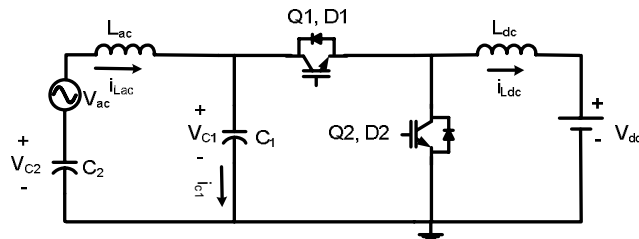


Fig. 4. Circuit inverter/rectifier proposed.

capacitor, leaving the  $C_2$  capacitor only with a DC voltage level (contrary to the proposed by Cáceres in [3], where the AC voltage is divided between both capacitors,  $C_1$  and  $C_2$ ). Thus, the condition below must be satisfied with a margin of security, in way that never  $V_{c2}$  is lower than  $V_{dc}$  (2).

$$V_{c2dc}^* > V_{dc} + V_{acp} \quad (2)$$

Therefore,

$$v_{c2}^*(t) = (V_{dc} + V_{acp}) + \Delta V_{dc} \quad (3)$$

With  $\Delta V_{dc}$  as the security voltage margin. It is considered that the AC mains voltage is  $V_{acp} \cdot \sin(\omega t)$ . The sum of the AC voltage and the voltage in the  $C_2$  capacitor is:

$$v_{ac}(t) + v_{c2}^*(t) = V_{acp} \cdot \sin(\omega t) + (V_{dc} + V_{acp} + \Delta V_{dc}) \quad (4)$$

therefore, the voltage in the  $C_2$  capacitor can be a DC voltage with minimum magnitude, definite by (2).

The reference function for the current is defined in (5).

$$i_{Lac}^*(t) = I_{Lacp}^* \cdot \sin(\omega t) \quad (5)$$

$L_{ac}$  is designed to filter the oscillations in high frequencies originated from commutation. Its impedance and the drop voltage in the AC mains frequency, in steady state are low. It is concluded then that the voltage  $v_{c1}(t)$  oscillates close to (6).

$$v_{c1}(t) = V_{acp} \cdot \sin(\omega t) + (V_{dc} + V_{acp} + \Delta V_{dc}) \quad (6)$$

DC level applied in  $C_2$  also is established in the  $C_1$  capacitor.

The duty cycle of the  $Q2$  switch is given by (7).

$$d(t) = 1 - \frac{V_{dc}}{V_{c2dc}^* + V_{acp} \cdot \sin(\omega t)} \quad (7)$$

For the energy balance the current in the  $L_{dc}$  inductor can be calculated by (8).

$$i_{Ldc}(t) = \frac{V_{c1}(t) \cdot (i_{Lac}(t) + i_{c1}(t))}{V_{dc}} \quad (8)$$

In steady state the current in the inductor is given by (9).

$$i_{Ldc}(t) = \frac{V_{c2dc}^* \cdot I_{Lacp}^* \cdot \sin(\omega t)}{V_{dc}} + \frac{I_{Lacp}^* \cdot V_{acp}}{2} \cdot \left. \begin{aligned} &\frac{(1 - \cos(2\omega t))}{V_{dc}} + \omega \cdot C_1 \cdot \left\{ \frac{V_{c2dc}^*}{V_{dc}} \right. \\ &\left. \cdot V_{acp} \cdot \cos(\omega t) + \frac{V_{acp}^2}{2 \cdot V_{dc}} \cdot \sin(2\omega t) \right\} \end{aligned} \right\} \quad (9)$$

The current  $i_{Ldc}$  is described by (9). It still has the excursions in high frequencies caused for the switching of



### A. System control of $i_{Lac}$ , $v_{c1}$ and $i_{Ldc}$

To carry out the control of these variables the control is implemented by sliding mode. The control for sliding mode extends to the properties of the control for hysteresis for an environment multi-variable, and it is possible to force the states of the system to follow a trajectory which is located on a convenient surface in the space of the states (sliding surface). With this purpose, each one of the zones of the space of the states, separate by the sliding surface, is associated with a state of the switches [3].

Two conditions are essential so that it has success in the implementation of a sliding regimen: the condition of existence and the condition of encounter. If it relates with the capacity of the system when beginning with initial conditions in  $t=t_0$ , it can find the sliding surface ( $\sigma$ ) in some  $t>t_0$ ; this refers to the maintenance of the sliding regimen after the encounter, or either, to the ability with that the system maintains the variable of state in a neighborhood enough next to  $\sigma$  [5]. The existence condition implies that around of  $\sigma$  the trajectories always must point with respect to own surface  $\sigma$ . Mathematically, this convergence is express by (18).

$$\lim_{\sigma \rightarrow 0^-} \left( \frac{d\sigma}{dt} \right) > 0 \quad \lim_{\sigma \rightarrow 0^+} \left( \frac{d\sigma}{dt} \right) < 0 \quad (18)$$

This indicates that, next to the sliding surface, if  $\sigma$  will have negative value, its derivative will have to be positive and if  $\sigma$  will have positive value, its derivative will have to be negative, so that in any situation the representative point if approaches to the null space  $\sigma = 0$  [5].

From (17) it looks for it error variation, subtracts in both sides the expression (17) the derivatives from the references from  $i_{Lac}^*$ ,  $v_{c1}^*$  e  $i_{Ldc}^*$ . The error is defined as  $\varepsilon = v - v^*$  and their derivatives as  $\frac{d\varepsilon}{dt} = \frac{dv}{dt} - \frac{dv^*}{dt}$  and disrespecting the derivatives of the references of the right side it is obtained in (19).

$$\begin{bmatrix} \frac{d\varepsilon_{iLac}}{dt} \\ \frac{d\varepsilon_{v_{c1}}}{dt} \\ \frac{d\varepsilon_{iLdc}}{dt} \end{bmatrix} = \begin{bmatrix} 0 & \frac{1}{L_{ac}} & 0 \\ -\frac{1}{C_1} & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} \cdot \begin{bmatrix} i_{Lac} \\ v_{c1} \\ i_{Ldc} \end{bmatrix} + \begin{bmatrix} 0 \\ \frac{i_{Ldc}}{C_1} \\ -\frac{v_{c1}}{L_{dc}} \end{bmatrix} \cdot \bar{\gamma} + \begin{bmatrix} -\frac{v_{ac} + v_{c2}^*}{L_{ac}} \\ 0 \\ \frac{V_{dc}}{L_{dc}} \end{bmatrix} \quad (19)$$

The parameter regent of the converter is  $\varepsilon_{iLac}$  (error in the current that circulates for  $L_{ac}$ ). To keep the current of the  $L_{ac}$  inductor enough near to its value of reference is the main objective of this converter. A good waveform of the  $i_{Lac}$  current and the difference of voltage in the capacitors  $C_1$  and  $C_2$  is expected. It fits, of this form, to the converter to diminish the possible discrepancies that appear. The error in the  $L_{dc}$  inductor is the main responsible for the determination of the instants of the commutations and  $\varepsilon_{v_{c1}}$  is the stabilizer parameter. This parameter is indispensable, therefore in this

application the reference is variable with the time.

Defined  $\varepsilon$ , as the error between the variable of control and its reference. Sliding surface is defined as  $\sigma$  (20).

$$\sigma = S \cdot \varepsilon = S_1 \cdot \varepsilon_1 + S_2 \cdot \varepsilon_2 + \dots + S_n \cdot \varepsilon_n \quad (20)$$

Choosing  $S$  invariant with the time, it is obtained:

$$\frac{d\sigma}{dt} = S \cdot \frac{d\varepsilon}{dt} \quad (21)$$

with  $S_1, S_2$  and  $S_3 > 0$ .

$$\sigma = S \cdot \varepsilon = S_1 \cdot \varepsilon_{iLac} + S_2 \cdot \varepsilon_{v_{c1}} + S_3 \cdot \varepsilon_{iLdc} \quad (22)$$

Substituting the variables of (19) in (21) and evaluating it meets expression (23).

$$\begin{aligned} \frac{d\sigma}{dt} = & S_1 \cdot \left[ \frac{v_{c1} - v_{ac} - v_{c2}^*}{L_{ac}} \right] + S_2 \cdot \left[ \frac{\bar{\gamma} \cdot i_{Ldc} - i_{Lac}}{C_1} \right] \\ & + S_3 \cdot \left[ \frac{V_{dc} - \bar{\gamma} \cdot v_{c1}}{L_{dc}} \right] \end{aligned} \quad (23)$$

State  $\gamma = 1$  ( $\bar{\gamma} = 0$ ) is associated with the increase of the energy in the system, therefore it is always applied that the representative point this below of  $\sigma = 0$ ; in opposed mode  $\gamma = 0$  is applied when the point it is located above of the switching line. Thus the following inequations are established.

When  $\gamma = 1 \Rightarrow d\sigma/dt > 0$  is shown in (24).

$$S_1 < \frac{L_{ac}}{v_{c1} - v_{ac} - v_{c2}^*} \cdot \left[ S_2 \cdot \frac{i_{Lac}}{C_1} - S_3 \cdot \frac{V_{dc}}{L_{dc}} \right] \quad (24)$$

When  $\gamma = 0 \Rightarrow d\sigma/dt < 0$  is shown in (25).

$$S_1 < \frac{L_{ac}}{v_{c1} - v_{ac} - v_{c2}^*} \cdot \left[ S_2 \cdot \frac{(i_{Lac} - i_{Ldc})}{C_1} - S_3 \cdot \frac{(v_{c1} - V_{dc})}{L_{dc}} \right] \quad (25)$$

It is considered initially that the  $L_{ac}$  inductor behaves as a current source  $i_{Lac}$  in order to determine the limit for  $\alpha$ . It is Defined as the reason between  $S_2$  and  $S_3$ , with  $Z_n = \sqrt{L_{dc}/C_1}$ . As in this in case  $S_1 = 0$ , can be calculated the value of  $\alpha$  and the restriction for  $S_1$ .

$$\gamma = 1 \Rightarrow \alpha < \frac{V_{dc}}{i_{Lac} \cdot Z_n^2} \quad (26)$$

$$\gamma = 0 \Rightarrow v_{c1} > V_{dc} + \max\{\alpha \cdot Z_n^2 \cdot (i_{Ldc} - i_{Lac}), 0\} \quad (27)$$

The  $S_1$  coefficient is finally defined, considering the maximum variation of  $|v_{Lac}| = |v_{c1} - v_{ac} - v_{c2}|$

$$S_1 \cdot |v_{Lac}| < L_{dc} \cdot \min \left\{ \left[ S_3 \cdot \frac{V_{dc}}{L_{dc}} - S_2 \cdot \frac{i_{Lac}}{C_1} \right], \left[ S_3 \cdot \frac{(V_{dc} - v_{c1})}{L_{dc}} - S_2 \cdot \frac{(i_{Ldc} - i_{Lac})}{C_1} \right] \right\} \quad (28)$$

The switching frequency for the sliding regime depends on the band of hysteresis used in the comparison of straight line  $\sigma$  with zero level.

$$f_{cd}(t) = \frac{d(t)}{\Delta\sigma} \cdot \left[ S_3 \cdot \frac{V_{dc}}{L_{dc}} - S_2 \cdot \frac{i_{Lac}^*(t)}{C_1} \right] \quad (29)$$

It is noted that the increase of the duty cycle as of the value of the AC current contribute positively for the increase of the frequency.

So that the value of  $f_{cd_{min}}$  really is verified, the band of hysteresis of the comparator must be chosen of appropriate form:

$$\Delta\sigma \leq \frac{d_{min}}{f_{cd_{min}}} \cdot \left[ \frac{S_2 \cdot V_{dc}}{L_{dc}} - S_1 \cdot \frac{I_{Lacp}^*}{C_1} \right] \quad (30)$$

### B. Control of $C_2$

In this case the classic control is used, through the theorem of the average value. It is substituted source  $V_{dc}$  and the  $L_{dc}$  inductor for constant current sources. The transfer function of the current  $i_{Lac}$  in function of the voltage in the  $C_2$  capacitor is shown in (31).

$$\left. \frac{\hat{i}_{Lac}(s)}{\hat{v}_{c2}(s)} \right|_{\substack{\hat{v}_{ac}(s)=0 \\ \hat{v}_{c1}(s)=0}} = \frac{1}{L_{ac} \cdot s} \quad (31)$$

Therefore, the variation of the current  $i_{Lac}$  with respect to the voltage of the  $C_2$  capacitor only depends on the filtering inductance of AC-side.

For this control the response it must be very slow (almost it continues), given that the voltage  $v_{c2}(t)$  of reference is a DC signal. As the transfer function already is an integrator, it can be used a proportional control, but a proportional integral control with filter for a better response will be used. The cut-off frequency chosen is near 10 Hz to obtain a slow response.

## IV. DESIGN AND SIMULATIONS

The converter in study has the following electrical characteristics:  $V_{dc}=100$  V;  $V_{ac}=155$  V; output power  $P=500$  W; minimum switching frequency 15 kHz. In agreement with established criteria the minimum voltage in the  $C_2$  capacitor must be 255 V(2). A safety margin of 45 V is applied, fixing the voltage of the  $C_2$  capacitor in 300 V. The  $C_1$  capacitor is calculated by (32) and the  $L_{dc}$  inductor by (33).

$$C_1 \geq \frac{I_{Lacp}^* \cdot d_{min}}{\Delta v_{c1_{max}} \cdot f_{cd_{min}}} = 15\mu\text{F} \quad (32)$$

$$L_{dc} \geq \frac{V_{dc} \cdot d_{min}}{\Delta I_{Ldc_{max}} \cdot f_{cd_{min}}} = 1.1\text{mH} \quad (33)$$

Following are showed the results obtained through numerical simulations. Considering  $S_3=0.244$ ,  $S_2=0.022$  and  $S_1=0.13$ . Change the operation mode it is simply necessary to change the reference signal of the current  $i_{Lac}$  and keeping the other unchanged parameters. Two high pass filters are used: for  $i_{Lac}$ , filter of second order,  $f_{pa}=1$  kHz,  $\xi=0.7$ ; for  $V_{c1}$ , filter of second order,  $f_{pa}=1$  kHz,  $\xi=0.7$ .

The results obtained in the operation as inverter are presented in the following figures. The voltages in the two capacitors are presented initially ( $v_{c1}(t)$  and  $v_{c2}(t)$ ), in Fig. 6. The current in the inductor is shown in Fig. 7. The current and voltage in the AC side is shown in Fig. 8, this present a THD $\approx$ 3.27% he current  $i_{Lac}$ , taking into account the firsts fortieth-ninth harmonics.

Inverting the signal of reference for  $i_{Lac}$ , the system starts to work as rectifier. The main results obtained by numerical simulations for the nominal load condition (2.5 kW) are shown in the figures that follow. Fig. 9 shown the voltage in the two capacitors. The current in the inductor is shown in Fig. 10. The current and voltage in the AC side is shown in Fig. 11, this presents a THD $\approx$ 2.04% he current  $i_{Lac}$ , taking into account the firsts fortieth-ninth harmonics.

## V. CONCLUSION

The presented converter is a new contribution to the family of the single-phase rectifiers with high power factor. This presents some advantages with respect to the already existing converters, these are:

- It operates, as rectifier or inverter, with the use of only a cell of conventional switching.
- It is bidirectional in current.
- The voltage output can be lower, equal or greater than the peak of the input voltage.
- The converter is able to maintain the input current,  $i_{Lac}$ , very close to the imposed sine reference (in phase with the input voltage), achieving a power factor next to the unit.

The control technical used shows some inconveniences because their nature is a control for hysteresis, the switching frequency is variable and depends on the operation point and the design of the control parameters that can be complex. That is compensated for a practical easy implementation.

The studied topology can find a large field of application in the generation of energy from sources of DC voltage (photovoltaic panels, for example). In the operation as rectifier, they offer a solution to connect it to the power system, without degrading the power factor, systems that demand DC voltage, especially in the cases where the levels of these are lower to the value of peak of the sinusoidal voltage available.

## VI. ACKNOWLEDGMENT

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## VII. REFERENCES

- [1] Cáceres Agelviz R. O.; Barbi, I. (1995). "A boost DC-AC converter: operation, analysis, control, and experimentation," *In: Intern. Conf. on Ind. Electron., Control, and Instrumentation – IECON (1995)*, Orlando, EUA. Anais. Piscataway, 1995. v.1,p.546-551.
- [2] Cáceres Agelviz R. O.; Barbi, I. (1999). "A boost DC-AC converter: operation, analysis, control, and experimentation," *IEEE Trans. On Power Electron.*, New York, EUA. 1999. v.14 ,p.134-141.
- [3] Cáceres A. (1997). "AC-DC converters Family, derivatives of basic converters DC-DC," *Thesis (Doctorate in Electrical Engineering, in portuguese)* – Technological Center, Institute of Power Electronic, Federal University of Santa Catarina.
- [4] Colling Eidt I.; Barbi, I. (2001). "Reversible Unity Power Factor Step-Up/Step-Down AC-DC Converter Controlled by Sliding Mode," *IEEE Trans. On Power Electron.*, 2001. v.16, No.2 ,p.223-230.
- [5] M.Carpita, M. Marchesoni, "Experimental study of a Power conditioning using sliding mode control", *IEEE Trans. Power Electron.* Vol.11, pp.731-742, Sept.1996.

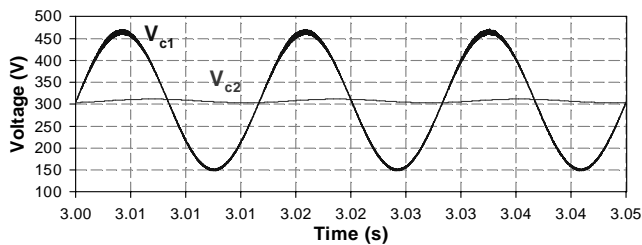


Fig. 6. Voltage on the capacitors  $C_1$  and  $C_2$ , in the operation as inverter.

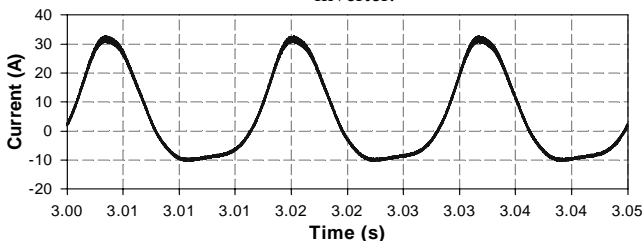


Fig. 7. Circulating current in the inductor  $L_{dc}$ , in the operation as inverter.

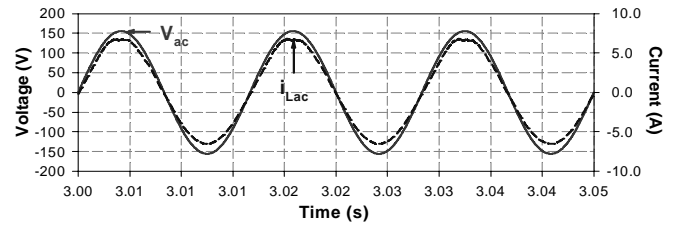


Fig. 8. Voltage ( $v_{ac}(t)$ ) and current ( $i_{Lac}$ ) in the AC side, in the operation as inverter.

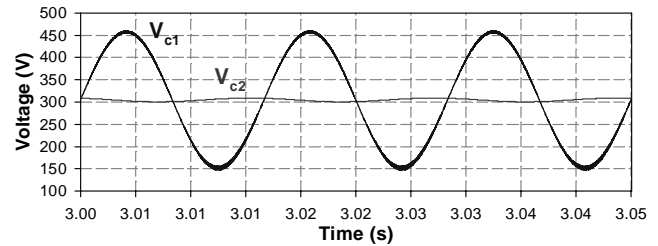


Fig. 9. Voltage on the capacitors  $C_1$  and  $C_2$ , in the operation as rectifier.

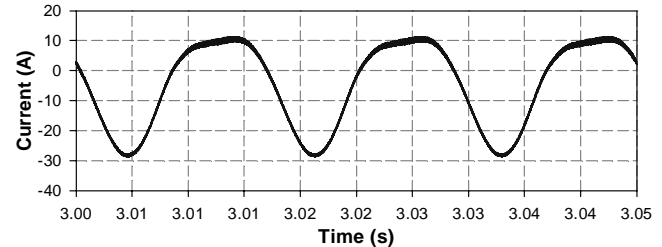


Fig. 10. Circulating current in the inductor  $L_{dc}$ , in the operation as rectifier.

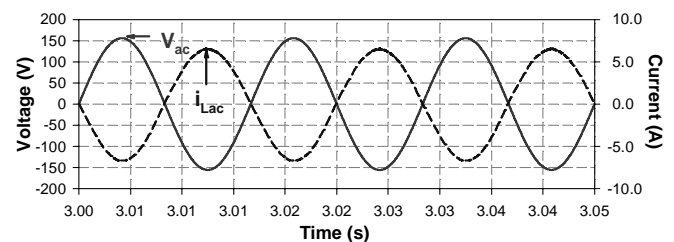


Fig. 11. Voltage ( $v_{ac}(t)$ ) and current ( $i_{Lac}$ ) in the AC side, in the operation as rectifier.